

Université d'Ottawa  
Faculté de génie

École d'ingénierie et de  
technologie de l'information



uOttawa

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University of Ottawa  
Faculty of Engineering

School of Information  
Technology and Engineering

**COURSE:** CEG2136/CEG2536  
Computer Architecture I  
Architecture des ordinateurs I  
**SEMESTER:** Fall 2008

**PROFESSORS:** Voicu Groza  
Aziz Abdesselam  
**DATE:** October 25, 2008  
**TIME:** 13h00 – 14h30

## MIDTERM EXAMINATION

**NAME and STUDENT NUMBER:** \_\_\_\_\_ / \_\_\_\_\_

### Instructions:

- Answer ALL questions on the questionnaire.
- This is a close-book examination.
- Use the provided space to answer the following questions. For your calculations you can use pages 6-8.
- Calculators are not allowed.
- Read all the questions before you start.

Q1. The range of signed integers  $N$  expressed in  $2$ 's complement representation that can be stored in a 10-bit register is:

1 point

- (a)  $-1024 \leq N \leq +1023$       (b)  $-1023 \leq N \leq +1024$       (c)  $-512 \leq N \leq +511$       (d)  $-511 \leq N \leq +512$   
 (e) None of the above

Q2. Identify the decimal number which is represented next in floating point with the IEEE 754 standard: 11000010100010101100000000000000

1.5 points

- (a)  $(-133.375)_{10}$     (b)  $(-69.375)_{10}$     (c)  $(-138.750)_{10}$     (d)  $(-34.6875)_{10}$     (e)  $(-8.671875)_{10}$

Q3. Give the best binary approximation of  $A = (26.6)_{10}$  and  $B = -(23.4)_{10}$  employing *signed 2's-complement representation* with 2 bits for the fractional part.

1.5 points

A =

B =

Q4. Two 6-bit registers contain two numbers  $X = 01010$  and  $Y = 10101$  (expressed in 2's complement representation). Using additions and 2's complementation only, calculate

- the sum ( $S = X + Y$ ) and
- the difference ( $D = X - Y$ )

1 point

1.5 points

Convert in decimal and write each intermediate and final result, to check the correctness of your assertions.

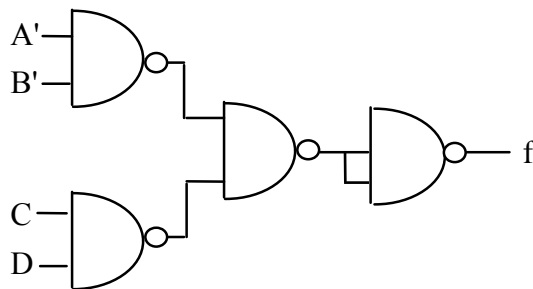
<u><math>S = X + Y</math></u>	<u>2's complement</u>	<u>Base 10</u>	<u><math>D = X - Y</math></u>	<u>2's complement</u>	<u>Base 10</u>												
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- Since both  $S$  and  $D$  have to be represented with 6 bits, indicate if overflow occurs; give the logic equation of a circuit which can detect such situations.

1 point

Q5. Which of the logic functions is implemented by the following circuit?

1.5 points



(a)  $f(A,B,C,D) = \Sigma m(4,5,6,7,8,9,10) + X(12,13,14,15)$

(b)  $f(A,B,C,D) = \Sigma m(4,5,6,8,9,10,14)$

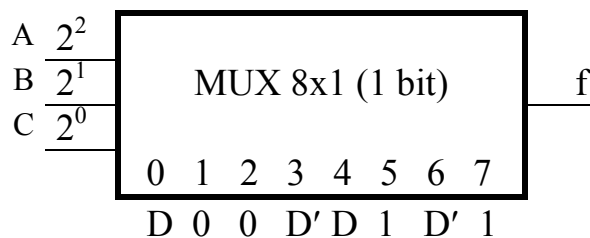
(c)  $f(A,B,C,D) = \Sigma m(0,1,2,3,6,7,14,15)$

(d)  $f(A,B,C,D) = \Sigma m(0,1,2,3,7,11,15)$

(e)  $f(A,B,C,D) = \Sigma m(4,5,6,8,9,10,12,13,14) + X(7,11)$

Q6. Which of the following logic functions is implemented by the given circuit?

1.5 points



(a)  $f(A,B,C,D) = \Sigma m(2,5,9,10,11,12,13,15)$

(b)  $f(A,B,C,D) = \Sigma m(0,7,8,10,11,13,14,15)$

(c)  $f(A,B,C,D) = \Sigma m(3,4,9,10,11,12,13,15)$

(d)  $f(A,B,C,D) = \Sigma m(3,5,6,7,8,12,13,15)$

(e)  $f(A,B,C,D) = \Sigma m(1,6,9,10,11,12,14,15)$

Q7. What is the capacity of a ROM, capable to implement three functions de six variables?

1.5 points

- (a) 8 words of 6 bits      (b) 16 words of 3 bits      (c) 32 words of 6 bits      (d) 64 words of 3 bits  
(e) None of the above

Draw a block diagram of your memory with the major components, indicating its inputs and outputs.

Q8.

- 1) - Draw the state diagram of the sequential circuit whose state table is given below

Present State      Next state

The State Diagram goes here:

1.5 points

A B C	$A^+B^+C^+$	JA	KA	JB	KB	JC	KC
0 0 0	1 0 0						
0 0 1	1 1 0						
0 1 0	0 0 1						
1 0 0	0 1 0						
1 1 0	0 0 0						

- Fill out the above table with the appropriate values for the JK flip-flops inputs such that the sequential circuit will observe the required transitions.

1.5 points

- Indicate the correct set of minimized equations of the JK flip-flops inputs from the following:

2 points

- (a)  $J_A = A'B'$ ,       $K_A = C'$ ,       $J_B = AB'C' + A'B'C$ ,       $K_B = BC'$ ,       $J_C = A'BC$        $K_C = A'B'C$ .  
 (b)  $J_A = A'B'$ ,       $K_A = 1$ ,       $J_B = A+C$ ,       $K_B = 1$ ,       $J_C = A'B$ ,       $K_C = 1$ .  
 (c)  $J_A = B'$ ,       $K_A = 1$ ,       $J_B = A+C$ ,       $K_B = 1$ ,       $J_C = A'B$ ,       $K_C = 1$ .  
 (d)  $J_A = A'B'$ ,       $K_A = A$ ,       $J_B = AC$ ,       $K_B = C'$ ,       $J_C = A'BC$ ,       $K_C = A'$ .  
 (e)  $J_A = B'$ ,       $K_A = A$ ,       $J_B = AC$ ,       $K_B = C'$ ,       $J_C = A'BC$ ,       $K_C = A'$ .

- 2) - If your circuit reaches by mistake any of the 3 states that are not used, determine their corresponding next state.

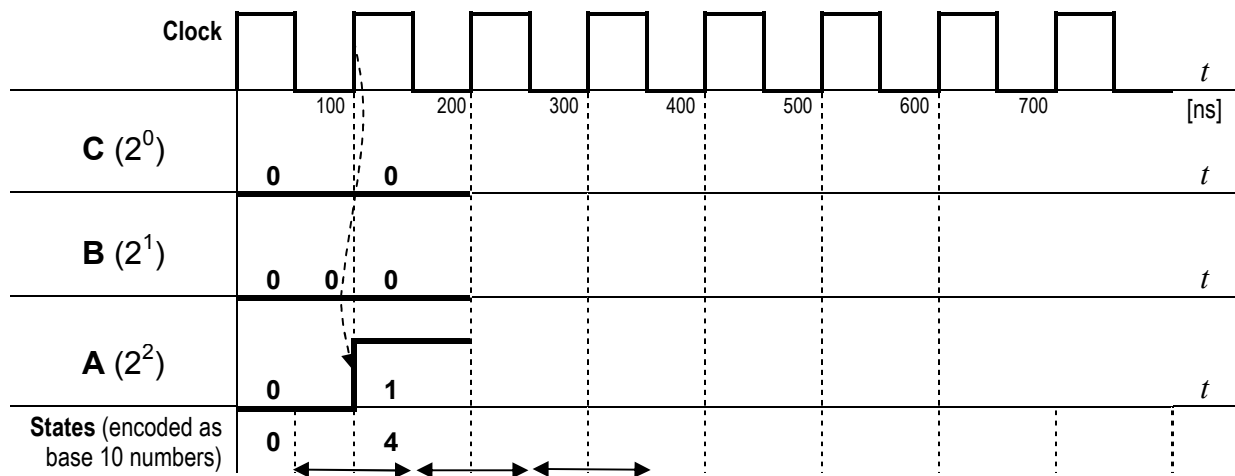
1.5 points

Present state	Next State

- Is your circuit auto-corrective?      Reply just with YES or NO

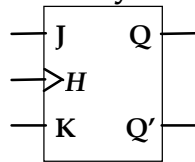
- 3) Draw the time diagram and give the states of the flip-flops' outputs through the first 6 clock pulses, assuming that their initial state (at  $t=0$ ) is 000 and they are triggered on the rising edge of the clock.

1.5 points



### Annex: JK flip-flop

Circuit symbol:



Characteristic Equation:

$$Q_{(t+1)} = JQ'_{(t)} + K'Q_{(t)}$$

Truth Table:

J	K	$Q_{(t+1)}$	
0	0	$Q_{(t)}$	No change
0	1	0	Q <- 0 (reset)
1	0	1	Q <- 1 (set)
1	1	$Q'_{(t)}$	Complement

Excitation Table

$Q_{(t)}$	$Q_{(t+1)}$	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

You can do your calculation here...  
(to be submitted but will not be marked)

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You can do your calculation here...  
(to be submitted but will not be marked)

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(to be submitted but will not be marked)